

p : price of a good

q : quantity demanded of a good

Demand function:

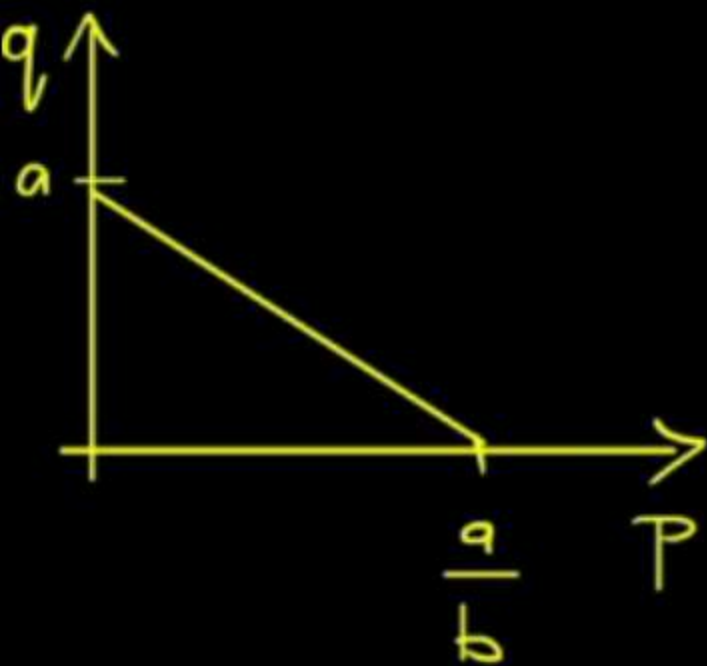
$$q = q^D(p)$$

Inverse demand function:

$$p = q^{D^{-1}}(q)$$

Example: linear demand function

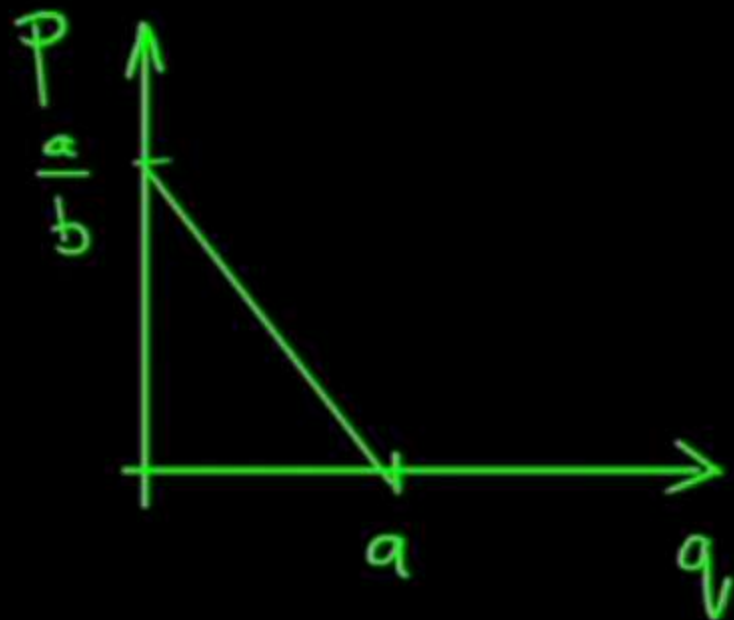
$$q = a - bp, \quad a > 0, b > 0$$



$$q = a - bp$$

$$bp = a - q$$

$$p = \frac{a - q}{b} = \frac{a}{b} - \frac{1}{b}q$$



Demand functions for alcohol

$$q_b(p_b) = 92p_b^{-0.36}$$

$$q_w(p_w) = 90p_w^{-0.70}$$

$$q_s(p_s) = 31p_s^{-0.68}$$

$$q_b(5) = 92 \times 5^{-0.36} \approx 52$$

$$q_b(10) = 92 \times 10^{-0.36} \approx 40$$

Source: Gallet, C. (2007) "The demand for alcohol: a meta-analysis of elasticities",
The Australian Journal of Agricultural and Resource Economics

$$q_b = 92 p_b^{-0.36}$$

$$p_b^{-0.36} = \frac{92}{q_b}$$
$$p_b(q_b) = \left(\frac{92}{q_b}\right)^{-\frac{1}{0.36}}$$

$$p_b(40) \approx 10, \quad p_b(52) \approx 5$$

$$p_b(31) = \left(\frac{92}{31}\right)^{-\frac{1}{0.36}} \approx \underline{\underline{20}}$$